



Introducing Kinematics with Robot Operating System (ROS)

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Introducing Kinematics with Robot Operating System (ROS)

Abstract

The study of Kinematics is essential to Robotics. A robot, to perform most applications needs to process positional data and transform data from one frame of reference to another. Robots have sensors, links and actuators each with its own frame of reference, so transformations between reference frames can be quite tedious. Traditionally Kinematics for robots is introduced to students with MatLab and the Robotic Toolbox. In this paper we examine the introduction of Kinematics for robotics with the features and tools available in the open source Robot Operating System (ROS). ROS implements tools for Kinematics transforms (tf) as a key part of the ROS Core Libraries. ROS defines robots with the Unified Robot Description Format (URDF) standard based upon Extensible Markup Language (XML). URDF is in many respects similar to Denavit-Hartenberg (D-H) Convention, but with significant additional enhancements.

We choose to introduce the Electronic Engineering Technology (EET) students to Kinematics and ROS so they would have greater insight into engineering projects involving robotics. We also found that using ROS in robotics projects not only makes the projects more interesting to students but, gives students an authentic experience with distributive systems and odometry sensors. Kinematics for robots uses Linear Algebra, Matrices, Natural logarithms (Euler's equation), Imaginary numbers and Trigonometry. The areas of mathematics we used to introduce kinematics for robotics to EET students are very similar to the mathematics to understand electricity, electric fields and circuit theory. We emphasize matrix operations, operations involving Trigonometric functions and imaginary numbers. This paper summarizes the result of this approach.

Introduction

The study and understanding of Kinematics is a tool in both industrial and mobile Robotics. A robot, to perform most applications needs to process positional data and transform data from one frame of reference to another. Robots have sensors, links and actuators each with its own frame of reference, so transformations between reference frames can be quite tedious. Software makes transforms easy to perform and automatic, but the student needs to understand Kinematics to use the software [1].

We designed the labs for EET students to give them basic kinematic concepts while gaining experience with ROS. We have added additional material for advanced students interested in robotics. In this paper we present enough kinematic theory to give the reader a good idea of what kinematic concepts are presented in the lab. In the detailed descriptions of the labs we also

covered how we used ROS to learn kinematics. The pre-lab materials and labs are available as free open source for readers who wish to know more.

The topics covered for the Kinematic Labs are depicted in Figure 1. Euler angles tend to be intuitive to describe robot motion but have issues when angles approach 90° . Quaternions are an alternative to using Euler angles but are not intuitive to use. We will treat Quaternions as black boxes and use Euler angles for our inputs to the robot model to have the best of both descriptions of rotation [2].

Joints used in our labs were Revolute or Prismatic. We can approximate other joint types in ROS using combinations of Revolute and Prismatic joints. We limited our joint types to keep the introduction to kinematics simple.

Joints in robots are usually combined in a series to form chains. Our Robot modeling software allows for chains to also be combined into tree like structures. A good example of a Kinematic tree would be a robot with two or more arms.

Forward Kinematics determines the position of the Robot given the joint rotations or distance for Prismatic sliding joints. Inverse Kinematics is more difficult than Forward Kinematics since we need to find one or more ways to move a Robot to a given point in space. Where there is usually a solution in Forward Kinematic problems there may be multiple or no solutions in an Inverse Kinematic problem.

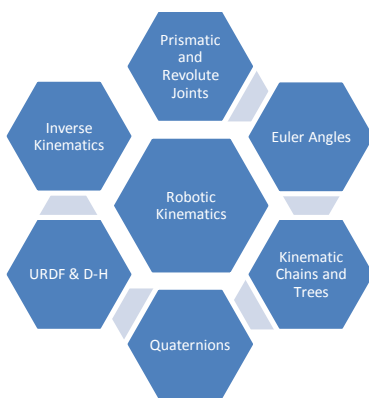


Figure 1 Robotic Kinematic Topic's for Labs

Robotic Operating System

We will explore Kinematics using software packages. ROS has a number of software packages that deal with Kinematics (see Figure 2). To demonstrate the Kinematic concepts from Figure 1, we needed to use more than one software package from Figure 2. RVIZ is a robot simulator that

can display a URDF robot model in 3D along with data from other sensors such as cameras. All the labs take advantage of RVIZ to demonstrate the six Kinematic concepts in Figure 1.

The tf software package provides a library of Kinematic routines that provides all the mathematical functions we need to transform Kinematic data from one frame of reference to another in our robot manipulators.

Transforms in ROS are made on positional data in both space and time. There are good tutorials in ROS on how data is transformed in the temporal domain. In this paper, we use examples and labs where the positional data is constant so we can ignore extrapolation in time. Time is important but we ignore it to “keep it simple” for students [3]. URDF is a XML modeling language capable of modeling most robots. Python is a programming language with interfaces to the ROS system.

Software packages in ROS are written mainly in Python, Lisp and C++. We will use Python interpreter much like a calculator. RVIZ GUI will display robot information and we will confirm the results using calculations made in Python.

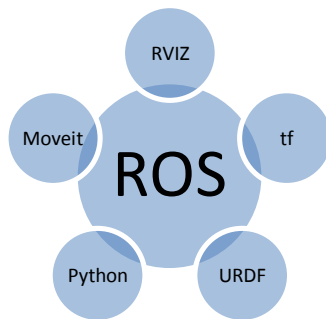


Figure 2 – Software Packages in ROS for Lab

MOVEIT is a fascinating software package for controlling robot arms and manipulator’s.

Each of the labs developed to introduce students to Robot Kinematics is listed in Table 1.

Lab	Title
1	RVIZ and PYTHON with Simple Robot Manipulator Model
2	RVIZ, TF and PYTHON with Aircraft Robot Model
3	URDF and Hydra Robot Models
3 EXTENT	Converting D-H Table to URDF Model
4	MOVEIT and Inverse Kinematics

Table 1 – Titles of Labs

Lab 1 deals with analyzing views of robot from different Frames of Reference and converting Quaternions to and from axis angle representation.

In Lab 2 the student converts Quaternions to and from Euler angles using the Python Programming Language.

In Lab3 students learn to read and write URDF files with the Linux Ubuntu screen editor gedit. The extension to Lab 3 exposes students to converting D-H tables to URDF files. Finally, students confirm there URDF model is correct with the RVIZ robot simulator.

Lab 4 gives the opportunity to run a number of inverse algorithms from OMPL using both the Willow Garage PR2 and 6R robot [4].

Please note Labs 1 – 3 deals with concepts in Forward Kinematics and Labs 4 in Inverse Kinematics.

Lab 1 RVIZ and PYTHON with Simple Robot Manipulator Model

In this Lab we will learn how to use the RVIZ Robot Simulator and convert Quaternions to/from axis angle representation. We will use the Python programming language to make our manual calculations and confirm ROS is working as expected (see Figure 1). Python is an interpreted language and supported by the Robotic Operation System (ROS).

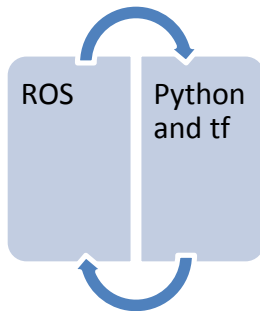


Figure 3 – Lab Setup

There are four sections to this lab:

- a) Setup and RVIZ features
- b) Converting from Quaternion to Axis Angle Representation
- c) Frames of Reference
- d) Robot Arm Movement Sequence

Setup will guide you through startup of RVIZ, Robot State Publisher and terminals. Features of the RVIZ display will be explored. We will convert Quaternions to Axis Angle representation to get useful information from the Quaternion. We will also change the Frames of Reference in the chain of links to take different measurements. Finally we will explore Sequences of moving arm joints to set the robot to different positions in 3D space.

Next is a screen shot of the RVIZ Robot Simulator showing the robot arm. The position is shown on the RVIZ screen along with relative position using Quaternions for the orientation. The Robot State Publisher screen is also displayed with sliders to control the robot arm [5].

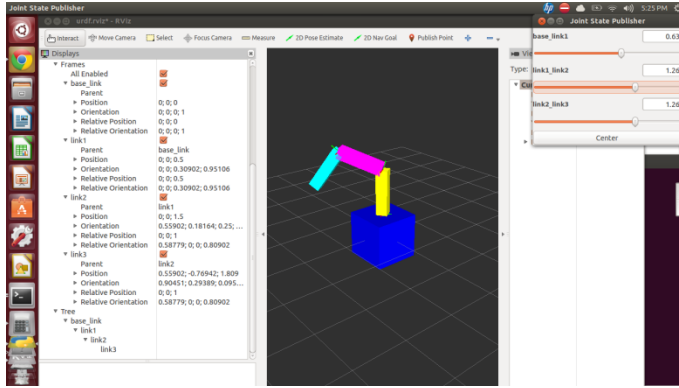


Figure 4 RVIZ Simulator and State Publisher Window

The second screen shot of the RVIZ Robot Simulator shows the robot arm visuals turned off to reveal the axis systems of each frame.

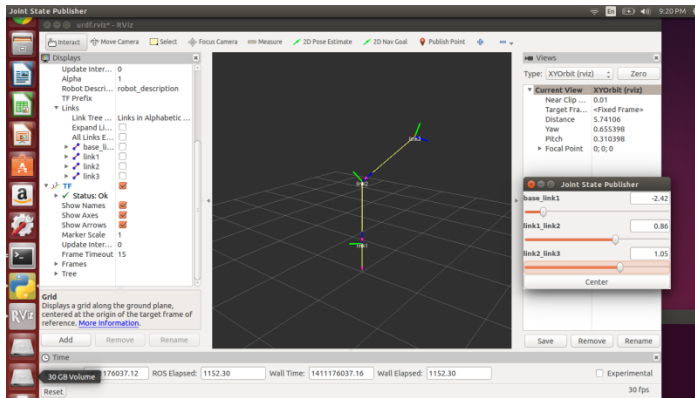


Figure 5 Joint Conventions and 3D Axis

Quaternions

Axis angle is somewhat intuitive and similar to Quaternions but in 3D. Axis angle can be converted to/from Euler angles to and from Quaternions. Eq. 20 through Eq. 30 converts the axis angle vector to a Quaternion [6].

$$q1 = \sin\left(\frac{\alpha}{2}\right) \cos(\beta_x) \quad (\text{Eq. 1})$$

$$q2 = \sin\left(\frac{\alpha}{2}\right) \cos(\beta_y) \quad (\text{Eq. 2})$$

$$q3 = \sin\left(\frac{\alpha}{2}\right) \cos(\beta_z) \quad (\text{Eq. 3})$$

$$q4 = \cos\left(\frac{\alpha}{2}\right) \quad (\text{Eq. 4})$$

The Quaternion is normalized so equation Eq. 5 is applies.

$$q1^2 + q2^2 + q3^2 + q4^2 = 1 \quad (\text{Eq. 5})$$

Equations 6 through 9 convert a Quaternion to axis angle vector.

$$\alpha = 2 \cos^{-1}(q4) \quad (\text{Eq. 6})$$

$$x = \frac{q1}{\sqrt{1-q4^2}} \quad (\text{Eq. 7})$$

$$y = \frac{q2}{\sqrt{1-q4^2}} \quad (\text{Eq. 8})$$

$$z = \frac{q3}{\sqrt{1-q4^2}} \quad (\text{Eq. 9})$$

The direction cosine angles can be found with the following equations:

$$\beta_x = \cos^{-1} x \quad (\text{Eq. 10})$$

$$\beta_y = \cos^{-1} y \quad (\text{Eq. 11})$$

$$\beta_z = \cos^{-1} z \quad (\text{Eq. 12})$$

EXAMPLE

Given the Quaternion:

$$q1 = 0.293802, q2 = -0.0957684, q3 = -0.294745, q4 = 0.904231$$

Note the Quaternion is normalized:

$$1 = q1^2 + q2^2 + q3^2 + q4^2 = 0.999999518$$

$$a = 0.427043673$$

$$\alpha = 2 \cos^{-1}(q4) = 0.8824416 = 50.56^\circ$$

$$x = 0.6829905, y = -0.2242590, z = -0.6901987$$

Note that $x^2 + y^2 + z^2 = 1$ and is thus normalized.

$$\beta_x = \cos^{-1} x = 46.5^\circ$$

$$\beta_y = \cos^{-1} y = 77.4^\circ$$

$$\beta_z = \cos^{-1} z = 133.6^\circ$$

Lab 2 RVIZ, TF and PYTHON with Aircraft Robot Model

In this Lab we will learn how to use the RVIZ Robot Simulator, Python Programming Interpreter and ROS tf library to study Euler angles. The Robot State Publisher allows for the Robot model in RVIZ to be controlled with sliders.

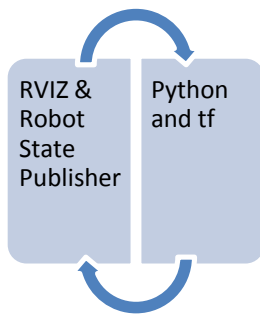


Figure 6 – Lab Setup

There are three sections to this lab:

- a) Euler Angles and Gimbal Lock
- b) Converting Quaternions to/from Euler Angles
- c) Frames of Reference and the tf Transform

Euler angles are expressed in terms of roll, pitch and yaw to specify the orientation of an aircraft. In ROS roll is a rotation about the x axis, pitch is a rotation about the y axis and yaw is a rotation about the z axis. All rotations in ROS follow the Right Hand Rule for direction of rotation [7].

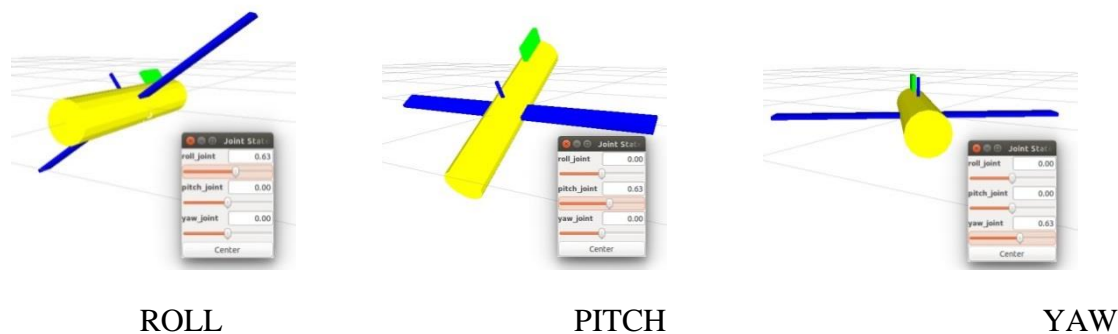


Figure 7 Roll, pitch and yaw of aircraft

Euler Angle Rotation Combinations

Proper Euler Angles	Tait-Bray Angles
R _Y R	R _Y P
R _P R	R _P Y
P _R P	P _R Y
P _Y P	P _Y R
Y _P Y	Y _P R
Y _R Y	Y _R P

Table 2 Euler Angle Combinations

Table 2 shows the combinations of Euler angles possible. Note, that Tait-Bray angles are also referred to as Euler angles.

The tf library provides two ways to convert Euler angles to Quaternions with any of the combinations in Table 2. The tf library can also provide a convenient conversion from Quaternions to Euler angles [8].

Euler angles are intuitive to use except there are issues with Gimbal Lock. Quaternions avoid the issues of Euler angles, but are difficult to visualize. We solve this dilemma by converting to and from Euler angles [9].

Using multiple Frames of Reference for a Robot makes it easy to calculate angles and distances from one point in the environment to another. We use the tf library in ROS to perform this task. We also learn some of the underlying concepts behind the magic of tf Transforms.

Lab 3 URDF and Hydra Robot Models

In this Lab we will learn how Unified Robot Description Format (URDF) describes robots and use it to design our own Robot. We will use the Ubuntu Linux editor gedit to modify and create URDF text files. We will use RVIZ a Robot Simulator and the Robot State Publisher in ROS to display and control our Robot Models [10].

There are five sections to this lab:

- a) URDF format and Simple Robot Model
- b) Ubuntu Linux Graphical Screen Editor gedit
- c) Hydra Robot Example
- d) Hydra Robots URDF models
- e) Design a Robot URDF model

URDF can be used to model a robot with links (members) connected by joints in a chain or tree. Most Industrial Robots can be modeled by chains of joints offset by links. Multi-arm robots can be modeled with a tree data structure of joints connected by links to a base link. We do not cover the transmission element at this point since all the robots we need are created by chains or trees. Other elements of URDF such as sensors are also not used.

There are two main types of URDF XML elements we need to create our robots links and joints. Link elements (or blocks) can contain elements for inertial properties, visual properties, and collision properties. Joint elements can also contain elements for origin, parent link name, child link name, axis of rotation/translation, calibration, dynamics, limit, mimic another joint and safety controller information.

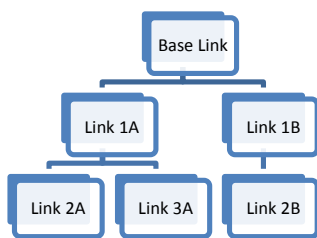


Figure 8 Kinematic Tree

The Kinematic Chain or Tree can be represented by a graph of links connected through joints between each Link and other links.

Link 1A is moved by the joint between the Base Link and Link 1A. Link 1A is connected to a joint between Link 1A and Link 2A that moves Link 2A. Link 1A is also connected to a joint between Link 1A and Link 3A which moves Link 3A. Each Link is moved by a single joint but may be connected to a number of joints that move other links. In URDF terminology multiple joints can be connected to one link, but the link can only be a Child in one of the joints connected to it and must be a Parent to all the other joints connected to it.

The Base Link is the first link in the tree and is special. The origin of the axis system to World coordinates x, y and z is determined from the Odometry Frame (/odom) and Map. In the example to follow our robot arm axis origin is located at World Coordinate 0,0,0.

It should be noted the students can get a graph of the Kinematic Tree or Chain with `urdf_graphviz` command typed in the terminal [11].

Link elements must have the “name” attributes for the link. The inertial and collision properties for the link are not included, except where it will be connected to a prismatic type joint. The visual information can be provided by specifying a rectangle, sphere or cylinder shape for the link or a mesh. Although the mesh produced by a Computer Aided Design (CAD) program can be very pleasing to the eye, we keep it simple with a rectangle or cylinder shape. As a

convention in the design of our robots for the labs we group together all the link elements to and then all the joint elements for readability of the URDF file [12].

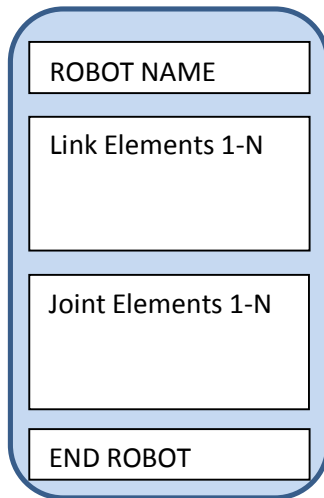


Figure 9 Types of URDF XML Blocks

The joint element has a name and an attribute for the type of joint. We only select a revolute, continuous or prismatic type for the joint. The ROS Continuous joint type in actuality is a revolute. In URDF a continuous joint is a revolute joint where the angle of rotation is 360° , where the revolute joint limits of rotation must be specified. The joint attaches a parent link to a child link. The child link can be a parent link to one or more other links in a chain or tree. The child link however can never be connected through a series of joints and links back to its parent link making a loop [13].

An example link element can be found in figure 10. We could have named the link anything we felt useful to identify it, since it was the second link in the chain we named it “link2”. We skip the inertial and collision information, not because it’s not useful but to keep the example simple. The visual element contains the geometry element which sets the type of display using the geometry element. The box element is inside the geometry element. The box element sets the x, y, z sizes of the rectangle. The visual also contains the material element which sets the color of the rectangle link. We set it to an arbitrary color to distinguish this link from other links in the RVIS simulator display.

```
<link name="link2">
  <visual>
    <geometry>
      <box size="1 0.25 0.25"/>
    </geometry>
    <origin rpy="0 1.571 0" xyz="0 0 0.5"/>
    <material name="linkc2">
      <color rgba="1 0 1 1"/>
    </material>
  </visual>
</link>
```

Figure 10 URDF XML Element Link Block

The visual also has the origin element inside it. The origin rotates the linkage visual display using roll, pitch and yaw angles. Roll is about the x axis, pitch is rotation about the y axis and yaw is rotation about the z axis. In the above example the rectangle is rotated 90° from the long side on the x axis to now point along the z axis. The link is offset ½ meter above the origin of the base link. The robot is actually buried in the floor in a hole ½ meter deep.

Syntax of the XML elements have the form “<label parameters>” followed by other elements and a “/>” or “</label>” [14].

Next, we examine a joint XML element in Figure 11. The joint must have some name which should make sense to identify where on the robot it resides. We choose in this example to use the label link1_link2, since we connect our link named link1 to our link named link2. The joint is a revolute type with no limits on rotation angle so we choose a continuous type. The parent link is link1 and the child link is link2.

The axis element specifies the axis the joint will revolve around which in this case is x. The origin xyz attribute is a offset of the joint from the parent joint origin to the child’s joint origin. The origin rpy parameter is a roll, pitch and yaw rotation on the child’s joint Frame of reference.

```
<joint name="link1_link2"
type="continuous">
  <parent link="link1"/>
  <child link="link2"/>
  <axis xyz="1 0 0" />
  <origin rpy="0 0 0" xyz="0 0 1.0"/>
</joint>
```

Figure 11 URDF XML Joint Element Example

The following command in the terminal window can be used in ROS to check the syntax of the URDF file:

```
roslaunch urdfdom check_urdf filename.urdf
```

Our robot URDF examples with prismatic joints are slightly more complex since prismatic joints require limits parameters and safety parameters not required for continuous joint type.

Lab 3 Extension – Converting D-H Table to URDF Model

Denavit-Hartenberg (D-H) Conventions ease the process of calculating the position and orientation of Frames in a Kinematic Chain [15]. As seen in the last section URDF can be used to model Robots that are Kinematic Trees. URDF does not require axis systems for Frames to only rotate about the Z axis. URDF actually uses arbitrary axis for Revolute or Prismatic Joints. However, we can tabulate the parameters of our URDF joint variables in a table analogous to D-H parameters.

To demonstrate we will use the axis system in Figure 12 to make the D-H table for the 3R robot similar to the 3R robot we saw earlier. The Θ variable represents rotation about the z axis of the joint. The d parameter is the distance along the z axis to the next joint. The d is a variable in the case of Prismatic joints. The a parameter is the distance of each common normal or the offset between joints. Finally the α parameter is the angle between the current joint i and the next joint i+1. The parameters in the D-H table can be translated to parameters in the URDF Joint element [16].

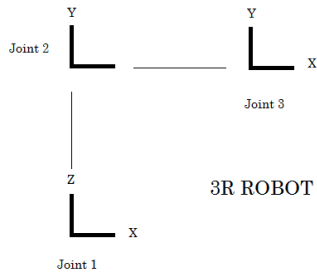


Figure 12 Axis 3R Robot

Note in Figure 12 has the y axis into the page for Joint 1 and z axis out of the page for Joint 2 and 3.

Link	θ_i	d_i	a_i	α_i
1	θ_1	d_1	0	90°
2	θ_2	0	a_2	0
3	θ_3	0	a_3	0

Table 3 D-H Parameters for 3R Robot

The parameters of the URDF Joint Elements can be enumerated in a Table similar in concept to the D-H table. For a simple Kinematic Chain there would be a single corresponding table to model the joints in the Robot. For a Kinematic Tree we could use multiple Joint Element Parameter tables to represent each Kinematic Chain in the Tree.

The d_i parameters will always be placed in the corresponding Joint + 1 z axis offset between Joint i and Joint i+1. The a_i parameter is the offset between Joint i and Joint i+1 along the x axis of Joint I and joint i+1.

We have to place the robot in World coordinates in ROS, so we will select a convenient orientation and origin to simplify calculations. We put the 3R robot at the origin of the World axis system and aligned with that axis system. This means instead of rotating Joint 2 by 90° we will rotate Joint 2 so the z axis will be out of the page. Joint 3 and 4 will also be rotated since 2 is attached to 3 and 3 is attached to Joint 4. Joint 4 is a Fixed type Joint and does not move. Joint 4 is included to show a3 parameter in the D-H table.

#	Joint Type	Joint Link #	Joint+1 Link #	x	y	z	Joint+1 Roll	Joint+1 Pitch	Joint+1 Yaw	Joint+1 Axis X	Joint+1 Axis y	Joint+1 Axis z
1	R	Base	1	0	0	d_1	0	0	0	0	0	1
2	R	1	2	a_2	0	0	90°	0	0	0	0	1
3	R	2	3	a_3	0	0	0	0	0	0	0	1
4	Fixed	3	4	0	0	0	0	0	0	-	-	-

Table 4 URDF Joint Element Parameters

Dummy URDF Link elements are set up with simple names such as Link_1, Link_2 etc. No information is needed in the URDF Link Element since we are not displaying visual elements of the Robot model in the Lab. We need a Base Link not included in D-H table to attach our robot model to the World Coordinates.

The parameters from the table to the URDF Joint Element are also straight forward. The x,y,z parameters corresponds to the origin xyz parameter in the URDF Joint element. The roll, pitch and yaw parameters corresponds to the origin rpy parameter in the URDF Joint element. Finally the axis parameters define a unit vector pointing along the z axis. Since this is a Revolute joint, the joint will rotate around the z axis.

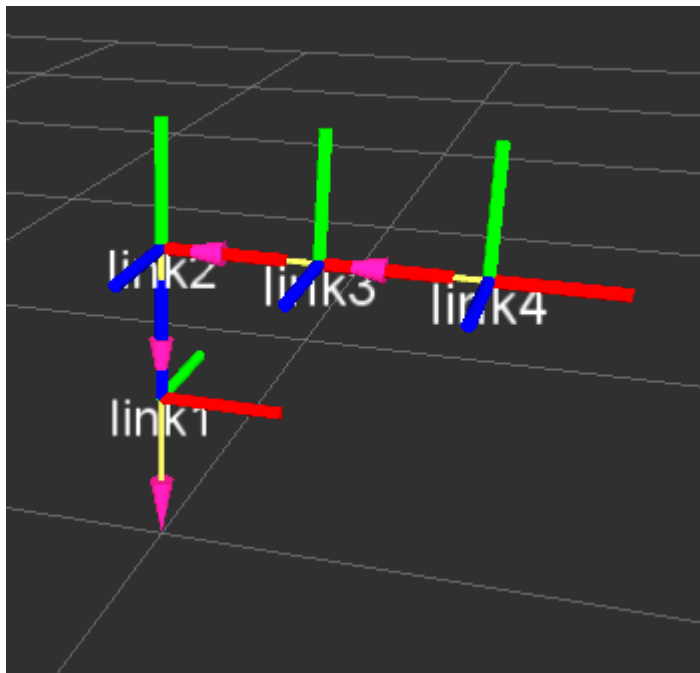


Figure 13 D-H 3R Robot Displayed in RVIZ

After students create the URDF Joint Element Parameter given the D-H table they perform, they convert it to URDF and display the results in RVIZ to confirm it matches the Fig. 12 axis system

orientation. The a_3 parameter is between Joint 3 and Joint 4. The Red axis is x, the Green axis is y and the Blue axis is z in Fig. 13.

Lab 4 MOVEIT and Inverse Kinematics

There are two sections to this lab:

- a) Setup Moveit
- b) Using Different Planning Algorithms to move robot

In this Lab we took advantage of existing demonstration software that uses the PR2 and 6R Robot. Students set the robots to different start and end states for the PR2 and 6R robots. Students can watch the robot perform the motion using the planning algorithm from the OMPL library and record the time it took to calculate a solution. There is an excellent tutorial that walks the students through the setup and use of the demo software [17].

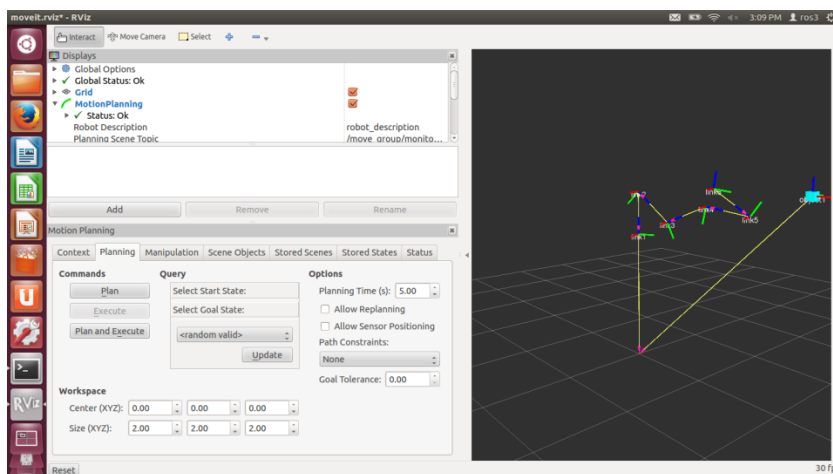


Figure 14 Demo Software Screen with 6R Robot

In the Lab students can select among the following planners to perform the path selected for the PR2 or 6R Robot [18]:

- 1) Bi-directional Kinematics Planning by Interior-Exterior Cell Exploration (BKPIECE)
- 2) Kinematics Planning by Interior-Exterior Cell Exploration (KPIECE)
- 3) Lazy Bi-directional Kinematics Planning by Interior-Exterior Cell Exploration (LBKPIECE)
- 4) Expansion Space Trees (EST)
- 5) Probabilistic Roadmap Method (PRM)
- 6) Transition-based Rapidly-exploring Random Trees (TRRT)

Building upon the RVIZ Plugin tutorial the student is presented with a problem requiring building a table for the selected algorithm using different Planning Groups and other Planning parameters. The student then records the results of the test in a table of planning parameters vs time and evaluate the results. The goal of the Lab is to give them some insight into the complexity of Inverse Kinematics.

Conclusion

We have presented the major features of the five labs developed to introduce our students to Kinematics using ROS. We are developing labs where students use accelerometers, and gyros to track real robots using ROS. The Introduction to Robotic Kinematics should provide the background to understanding Kinematic aspects of these labs.

The Robot Toolbox provides a powerful system for introducing students to Robotic Kinematics [19]. However for EET students teaching kinematics on ROS is more efficient, since students use ROS on other projects.

Information to obtain the free Open Source labs outlined in this paper can be found at reference [20].

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