

# Using Computer Simulations in a Freshman Mechanical Engineering Course to Make Informed Design Decisions

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#### Abstract

In this complete evidence-based paper, it will be shown how computer simulations can be introduced in a freshman mechanical engineering course and how students can use computer simulations to make informed design decisions. Freshman-level engineering students may have insights about the workings of mechanical systems even though they may not be versed in the mathematical descriptions of such systems. The motivation for this work is three-fold: (1) allow freshman students to apply and expand their insights into mechanical systems without the need for mathematical descriptions which they may not yet be prepared to understand; (2) expose students to computer simulations at an early stage of their curriculum to solve engineering problems; and (3) offer opportunities for team work within the course on a large scale (200+ students) with reasonable resources. This paper shows how the course and computer simulation activities are set-up and administered and it provides a description of the design activity. Some samples of student work are provided. Student work is assessed based on their ability to: (1) specify design goals, (2) describe the design alternatives, (3) list relevant assumptions and constraints, (4) provide a procedure for using computer simulations to obtain data, and (5) use simulation data to make design decisions. There are several benefits to the method described in this paper including allowing instructors to cater to diverse student interests with limited resources. Specifically, it allows students to expand on course topics easily and meaningfully, allows students to apply existing knowledge and experience to create something new, motivates students, and interests them as they prepare for their future engineering courses.

### 1. Introduction

Modern engineers can make important decisions about the design of complex systems using computer simulations. When applied properly, simulation results can be leveraged to validate an engineer's ideas, which can lead to new designs and improved systems. Creating, running, and post processing basic simulations is possible using Computer-Aided Design (CAD) software, a desktop computer, and relevant training.

Computer simulations are incorporated into a first-year introductory course in the mechanical engineering curriculum at the University of Texas at Dallas. Many first-year engineering students taking this course have insights about the workings of mechanical systems even though they may not be versed in the mathematical descriptions of such systems. Computer simulations can help these students make engineering decisions as they compare the numerical results based on different designs they are considering. More importantly, analyzing simulation results and errors generated during the simulation process ignites the student's curiosity to learn engineering

concepts that are covered in an elementary form in this class and in more detail in upper-level classes. Students are taught the basics of using computer simulations in this class in a team-based design approach. Past work has shown that incorporating team-based design projects into first-year engineering courses is beneficial since it increases motivation and improves retention [1-3].

In this work, a computer simulation is defined as a program that accepts inputs and performs calculations based on a mathematical model of a system with the intent of understanding the behavior of said system [4-5]. In our freshman-level course, students used SolidWorks threedimensional (3D) CAD software to simulate kinematic motion, structural integrity, fluid flow and heat transfer processes (conduction and convection). These types of computer simulations are often introduced in courses taken later in a typical mechanical engineering curriculum [6-7] but we wanted to introduce students to these simulations at the freshman-level to motivate and inform students in a meaningful way about future engineering courses. Research has also indicated that computer simulations can be as effective at demonstrating concepts as experiments since they highlight the important aspects being studied and omit those that are not [8-11]. An added benefit for instructors is providing an opportunity for team-based work that can be executed on a large scale (200+ students) with resources available in typical engineering departments (i.e. a computer lab equipped with CAD software).

The work of Carruthers and Clingan [12] introduces first-year students to Computational Fluid Dynamics (CFD) simulations to solve an open-ended design problem. They note that even though students lack the necessary math background and fluid mechanics concepts, and have never used CFD software before, their students were able to overcome these limitations by being introduced to the concepts in a basic form and being exposed to guided examples to become familiar with the CFD environment. In order to reduce the misuse of CFD software by their students, they provided them a list of problem-solving tactics outlining when to use certain constraints and when not to trust their CFD solutions. In our work, we follow a similar approach in that our students are provided a foundational understanding of the concepts bridging their knowledge from calculus-based physics and being provided guided examples illustrating how to setup and run various types of simulations. We also minimize the potential misuse of the simulations by having instructors and Graduate Teaching Assistants (GTAs) oversee the student's simulation setup if students express concern or directly ask for help. Additionally, basic concepts in motion and power transmission, fluids, thermal and energy systems, forces in structures, materials and stresses are discussed in an elementary level in the introductory book by Wickert and Lewis [13] while Oakes and Leone [14] provides basic concepts in visualization and graphics, statics and dynamics, and thermodynamics. Using resources such as these, can help instructors facilitate the discussion of these concepts - some of which may be new to the firstyear student.

For our freshman course, the Course Learning Outcomes (CLOs) are written so that students completing the course are able to do the following: (1) explain concepts in mechanical design, forces and stresses, engineering materials, motion and power transmission, and thermal and energy systems; (2) develop problem-solving and communication skills; (3) function as a team on group projects; and (4) explain how continued education and knowledge of contemporary issues is important for the long-term effective practice of engineering. Team-based, design activities and projects making use of computer simulations have been important instruments to assess these CLOs (see 'Results').

This paper includes a description of the class and how it is administered, a description of the design project and its assessment, and samples of student work.

### 2. Methods

The class is typically taken during the second-semester (Spring), freshman year and focuses on design-related activities relevant to the mechanical engineering profession including CAD, forces on structures, thermal energy and fluid systems, and mechanical components [15]. The class has a 50-minute, weekly lecture attended by all students (200+) and a 1-hour and 40-minute, weekly lab capped at 50 students. In a typical Spring semester, five labs are offered. Each lab has one faculty instructor and two GTAs or upper-level Undergraduate Students (UGS) helping provide frequent, prompt, and constructive feedback as recommended by Ambrose and Amon [2]. The work performed in the labs is team-based and attendance is taken.

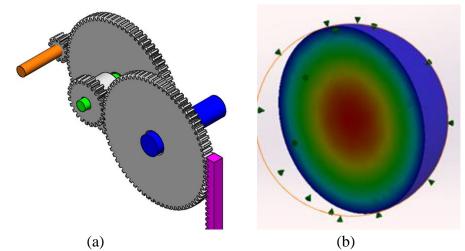


Figure 1. (a) Motion simulation of a geared mechanism. (b) Thermal analysis simulation of sphere cooling under forced convection.

Throughout the semester, students work on activities in the lab where they are taught how to create 3D part and assembly models using SolidWorks [16], how to set-up and run a motion simulation of a geared mechanism [17] (Figure 1(a)), how to perform force analysis of simple

structures [18], and how to set-up and run a thermal analysis simulation on a sphere being cooled under forced convection [19] (Figure 1(b)). As previously mentioned, SolidWorks is primarily used to perform these simulations but Matlab is also used. These activities are used to teach the students how to properly set-up their simulations. The activities also allow the students to match the concepts discussed in the lectures with the data they obtain through the simulations. The use of SolidWorks is taught throughout the semester.

The final design project is an opportunity for the students to further explore any of the course topics they found interesting. For the project, students are asked to do the following:

- select a mechanical system and research it (how it works, how it is modeled, etc.);
- model the system in SolidWorks (students can use 3D component models from online catalogs, e.g. gears, shafts, and bearings);
- select one or two design parameters that are significant to the system chosen;
- and investigate the effects of modifying the design parameters.

The choice of system is up to the students but they are advised against selecting systems that are too complex. Students can investigate different fin designs to cool an object, design a small toy car with a gear train, design a structural component, or design a new tool. Projects are assessed based on the following criteria:

- c1. **Design Goals** Describe what you hope to accomplish.
- c2. **Design Alternatives** Explain what parameters will vary between the design alternatives considered and which parameters will remain the same.
- c3. Assumptions and Constraints Explain what the limitations of the computer simulations you will perform are.
- c4. Simulation Procedure Explain how data is obtained.
- c5. **Design Decision** Select a final design using the simulation data of each of the design alternatives.
- c6. **Creativity** Creative application of course topics.
- c7. **Complexity** Undertaking a challenging simulation or mechanical system.

The assessment results are provided in 'Results' below. It should be noted that criterion c6 was strongly encouraged and, as previously mentioned, criterion c7 was advised against due to time limitations.

The example provided to the students is presented in Appendix A. This example involves convective cooling of an object with fins. The aim is to mimic how a computer chip can be cooled more efficiently.

Students were given two weeks of lab time to work on the design project (Figure 2, a). Students are also given access to the computers and are encouraged to work outside of lab time (Figure 2, b) to complete this project. The labs are administered in a space dedicated to supporting first-year mechanical engineering students. This space is designated as a dry lab and currently supports up to 50 students. In the space, each team of two students uses a large worktable, a computer, and a toolbox. The GTAs and UGSs continually move around the lab and stop to offer help and advice during the lab hour and multiple office hours. This makes the students more willing to ask questions.



Figure 2. Students working in the Mechanical Engineering Freshman Studio during (a) a regular lab session and (b) outside lab time.

### 3. Results

The design project was implemented with no issues in a class of 213 students in the Spring 2018 semester. The students worked in teams of two during two lab sessions. Based on instructor observations, it is recommended that the first lab session should be used to determine the design goal, design alternatives, and assumptions and limitations of the simulations that will be used to collect data. The second session should be used to complete the simulations. The final report can be completed at home or, if the schedule permits, a third lab session can be provided to the students to complete this task in the lab.

Criteria c1 to c7 were used to evaluate the student projects. Each project was evaluated by an instructor based on Table 1. The project evaluations discussed in this paper were independent of the grading rubric implemented; however, the lower a criteria evaluation for a project, the higher the point deductions. Projects that include a simple modification of the previous simulation activities or of the instructor example (see Appendix A) were given low marks for creativity. For

example, one team followed the instructor's example but looked at different fin shapes instead of the number of fins. This team worked on an unoriginal design but they were able to draw nice conclusions from their simulation data and were given high marks for their design decision. Namely, this team was able to describe how surface area to volume ratio of the fins is important to consider but shapes having high ratios might be harder to manufacture. An example with high marks for creativity and making an informed design decision is the coffee pot redesign, which will be described below. This team conducted good research and applied the thermal simulation they learned in class in a creative and original manner. The samples of student work provided later in this section will provide additional examples of students making informed design decisions.

| Criteria                 | Evaluation  |  |  |  |  |  |
|--------------------------|---|--|--|--|--|--|
| c1. Design Goals         | 1 – Design goals not presented  |  |  |  |  |  |
| C1. Design Goals         | 5 – Clear description of design goals   |  |  |  |  |  |
|                          | 1 – Not evident what design parameters were considered                              |  |  |  |  |  |
| c2. Design Alternatives  | 5 – Clearly explained all design parameter values including those that vary between |  |  |  |  |  |
|                          | design alternatives and those that are constant                                     |  |  |  |  |  |
| c3. Assumptions and      | 1 – Lacked all assumptions or constraints necessary for their simulation            |  |  |  |  |  |
| Constraints              | 5 – Clearly described all necessary assumptions and constraints                     |  |  |  |  |  |
| c4. Simulation Procedure | 1 – Not evident how data was collected  |  |  |  |  |  |
|                          | 5 – Followed assumptions and constraints, and clearly described how data was        |  |  |  |  |  |
|                          | collected   |  |  |  |  |  |
| c5. Design Decision      | 1 – Did not make any decision   |  |  |  |  |  |
|                          | 5 – Able to make a clear design decision based on simulation data                   |  |  |  |  |  |
| c6. Creativity           | 1 – Not original; for example, did a simple modification to professor's example     |  |  |  |  |  |
|                          | 5 – Students applied course topics in an original and creative way                  |  |  |  |  |  |
| c7. Complexity           | 1 – Very simple simulation and mechanical system                                    |  |  |  |  |  |
|                          | 5 – Undertook a challenging simulation or mechanical system                         |  |  |  |  |  |

Table 1. Evaluation of criteria made on a 5-point Likert scale.

Table 2. Statistical analysis of criteria (c1 - c7). Sample size is n=99.

| Criteria | Average | Standard  | Pearson Correlation Coefficient, p |        |        |        |        |        |        |
|----------|---------|-----------|------------------------------------|--------|--------|--------|--------|--------|--------|
|          |         | Deviation | c1                                 | c2     | c3     | c4     | c5     | сб     | c7     |
| c1       | 4.0808  | 1.0368    | -                                  | 0.4919 | 0.1933 | 0.3202 | 0.3263 | 0.3436 | 0.4815 |
| c2       | 3.5859  | 1.1867    |                                    | -      | 0.3386 | 0.3828 | 0.4777 | 0.2116 | 0.3524 |
| c3       | 3.2828  | 1.1069    |                                    |        | -      | 0.5205 | 0.4447 | 0.2926 | 0.1154 |
| c4       | 3.6869  | 1.3065    |                                    |        |        | -      | 0.6010 | 0.2106 | 0.1925 |
| c5       | 3.5657  | 1.3714    |                                    |        |        |        | -      | 0.4135 | 0.5189 |
| сб       | 3.1010  | 1.2657    |                                    |        |        |        |        | -      | 0.5952 |
| c7       | 3.2930  | 1.3420    |                                    |        |        |        |        |        | -      |

Table 2 shows the statistical analysis of the seven criteria (c1 - c7). The average and standard deviation for each criteria are given, as well as the correlation between them. Of particular interest in this work was the correlation between properly setting up the simulation procedure and their ability to make an informed design decision (i.e., correlation between criteria c4 and

c5). For this we observed a p=0.6010 indicating a strong positive correlation between these criteria.

The assessment results for c4 and c5 are plotted in Figure 3. In this plot, the bubble size is proportional to the number of instances. The data point (c4, c5) = (5,5) occurred 24 times out of 99 projects evaluated (~24%) and correspond to the largest bubble. These projects were deemed the most successful projects evaluated. An expected trend line is also shown in this figure. The slope of the trend line illustrates that projects that had issues with the simulation procedure were also more likely to have issues making an informed design decision.

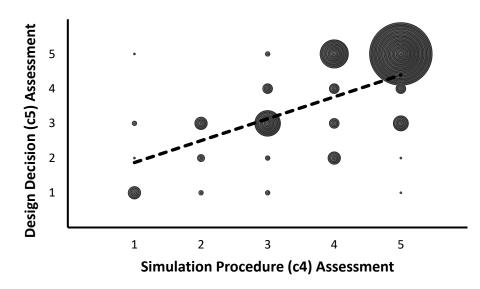


Figure 3. Design decision vs simulation procedure (p=0.6010).

The assessment results also showed that, overall, students creatively applied the course topics to challenging problems which indicated a good understanding of the course topics. Their ability to work in teams to articulate goals, parameters, assumptions, etc. was also an indication of their problem-solving and communication skills. Overall, the assessment results indicated a mastery of the course CLOs.

Samples of student work are described next. These samples illustrate the diversity of projects the students chose to work on.

An example of student work related to thermal energy systems is provided in Figures 4 and 5. The goal set by the students was to redesign a coffee pot to heat its contents faster. Figure 4 shows 3D solid models developed by the students of a standard coffee pot and heating element (Figure 4(a)) and their suggested design (Figure 4(b)). Figure 4(a) was used to provide a baseline for comparison. Figure 5 shows the thermal analysis results of the coffee pot's liquid contents, which were modeled as a solid for their simulation. One modification the instructors would have liked to see was to have the students keep the same volume of the coffee pot contents to get a

better comparison. Nonetheless, the students provided an excellent demonstration of thermal energy concepts, proficiency in running a simulation, and were able to make an informed design decision based on simulation data and not simply intuition.

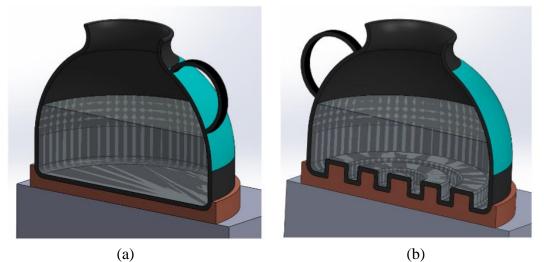


Figure 4. Cross-sectional views of (a) a standard coffee pot and (b) the suggested design. The heating element is also shown.

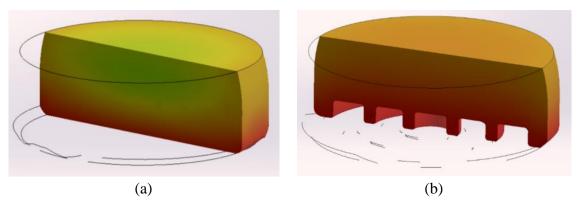


Figure 5. Thermal simulation results of the coffee pot contents for (a) the baseline design and (b) the suggested design.

An example of student work related to gears and motion simulation is provided in Figure 6. The goal of this team was to control the speed of a turntable to three different speed settings (33.3 RPM, 45 RPM, and 78 RPM) with a motor having a constant speed. The students searched the McMaster-Carr online catalog [20] for their gears, performed hand calculations, and performed motion simulations to verify their results. Since this catalog has a limited number of gears, the challenge was selecting the gears to get as close to the desired speeds as possible. The students were able to achieve turntable speeds of 33.3 RPM (exact match), 43.8 RPM (2.7% lower than desired) and 75 RPM (3.8% lower than desired) using the same speed at the pinion. This team

was able to make informed component selections based on realistic 3D CAD models of gears obtained from the McMaster-Carr catalog and simulations to validate their results.



Figure 6. Turntable with adjustable speed.

Another example is shown in Figure 7. This team drew on the experience of one of the team members as a mechanic to come up a new tool design. The team's goal was to combine the three most common tools the student used to into one, saving time by eliminating the need to go back-and-forth to the toolbox. The students performed stress analysis on designs of different materials. The stress analyses performed by this team allowed them to validate their model's dimensions (feature sizes) and their material choice.



#### Figure 7. Multi-purpose automotive tool.

In other design projects, students investigated fluid flow within a pipe with various types of obstructions, simulated different truss geometries under applied loads, looked at stress and displacement of different beam designs, simulated planetary gear trains for use in bicycles, and investigated different koozie designs to keep a beverage cold. Overall, we saw a wide range of applications making use of the computer simulations they were given as guiding examples, which was one of our expectations when we introduced this project. However, we also observed that there were many projects related to the example provided to the students presented in Appendix A. We saw many variations of this including changing the shape, number, and size of the fins or of the object that was cooled using the fins.

Another interesting outcome was that the instructors noticed an increase in the number of questions regarding when – and in which courses – they would see a particular topic again. This was particularly meaningful to the instructors as important instructor objectives are to get students motivated, interested, and prepared for their future engineering courses and ultimately professional careers.

#### 4. Conclusions

In this paper, a design project for a freshman mechanical engineering course based on computer simulations is described. The project was successfully administered to 200+ students with limited resources. Throughout the semester, students were given team-based, design activities to learn how to set-up and run various types of computer simulations in SolidWorks and were provided with supporting information on the concepts in the lectures. The students applied this knowledge in their final design project. The topic of the design project was selected by the students but requirements were specified by the instructors.

Overall, the instructors saw a large variety of projects dealing with machine components, tool design, fluid flow, heat transfer, and structural design. Students were able to expand on the course topics in an easy and meaningful manner. Some students applied existing knowledge and experience to create a new design while others used this opportunity to work on problems they would see in future engineering courses. Important to all projects was the student's ability to use computer simulations and 3D models to make informed design decisions, which was shown through the statistical analysis of project assessments.

In future work, the authors would like to investigate the long-term effects on student interest.

#### 5. Acknowledgements

The authors would like to thank students Rebecca Choate, Eben Oliver Pfeil, Abhishek Srinivas, Sai Siddardh Dommeti, William Scott and Dylan Newbery for allowing us to use their models for this paper. The photographs of the Freshman Design Studio are courtesy of SmithGroup.

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## Appendix A

- **Goal**: Determine how long it takes to cool the center of a rectangular object to 300K if it starts at a uniform temperature of 473K and a fan is blowing air over it. To help cool the object faster, cylindrical-shaped fins are added to increase the surface area thus increasing the rate of heat that will be extracted due to convection.
- **Design Alternatives**: The number of fins will be modified to determine the effects on the time it takes to cool the center of the object. The time to cool will be determined for 0, 12, 20, 28, and 32 fins. The alternative with 0 fins becomes the baseline to compare the other alternatives. The size of the rectangular object and each individual fin will remain constant. Additionally, the material (aluminum 1060), the convection coefficient (40 W/m^2-K), the initial uniform temperature of the object (473K), and the ambient temperature of the air (273K) will also remain constant.
- Assumptions and Constraints: The object is a rectangular shape (1 inch by 0.5 inch by 0.2 inch) and fins are cylindrical (0.05 inch diameter by 0.2 inch length). The entire object (rectangle and fins) is made of a single material. The object does not have any internal

sources of heat. The SolidWorks thermal simulation parameters are as follows: 600 seconds total simulation time, 10 second time step, and default mesh settings.

- **Procedure**: The following steps are taken to collect necessary information.
  - 1. Create a 3D SolidWorks model of the object with 0 fins.
  - 2. Run thermal simulation and determine the time to cool. Figure 8 shows how the center of the object cools over time and the temperature distribution of the object.
  - 3. Modify the 3D model to 12 fins and repeat Step 2.
  - 4. Repeat Step 3 for 20 fins, 28 fins, and 32 fins.
  - 5. Plot time to cool versus the number of fins (see Figure 9).
- **Design Decision**: Based on the results shown in Figure 9, we see diminishing returns with the number of fins and after 28 fins there is no significant change in the time it takes to cool the center of the chip. Our final design would have 28 fins.

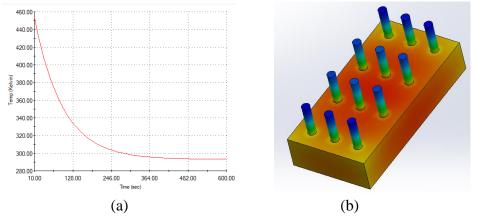


Figure 8. (a) Plot of maximum temperature of the object versus time for the case of 12 fins. Maximum temperature occurs at the center of the computer chip. (b) Temperature distribution over the object for the case of 12 fins. Through conduction, heat is transferred from the center of the object to the fins.

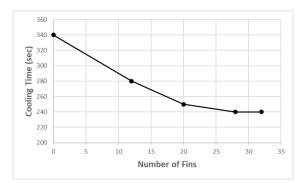


Figure 9. Plot of cooling time versus number of fins.